

## Decay modes of the Hoyle state in $^{12}\text{C}$

H. Zheng,<sup>1</sup> A. Bonasera,<sup>1,2</sup> M. Huang,<sup>3</sup> and S. Zhang<sup>3</sup>

<sup>1</sup>*Laboratori Nazionali del Sud, INFN, via Santa Sofia, 62, 95123, Catania, Italy*

<sup>2</sup>*Cyclotron Institute, Texas A&M University, College Station, TX 77843, USA*

<sup>3</sup>*College of Physics and Electronics Information, Inner Mongolia University for Nationalities, Tongliao, 028000, China*

Recent experimental results give an upper limit to the direct decay of the Hoyle state into  $3\alpha$  of equal energy respect to the sequential decay into  $^8\text{Be}+\alpha$  less than 0.043% (95% C.L.). We performed one and two-dimensional tunneling calculations to estimate such a ratio and found it to be more than one order of magnitude smaller than experiment depending on the strength of the nuclear force [1]. This is within high statistics experimental capabilities. Our results can also be tested by measuring the high excitation energy states of  $^{12}\text{C}$  decay modes where the ratio of direct to sequential decay might reach 10% at  $E^*(^{12}\text{C})=10.3\text{MeV}$ . The link between a Bose Einstein Condensate (BEC) and the direct decay of the Hoyle state is also addressed. We discuss a hypothetical ‘Efimov state’ at  $E^*(^{12}\text{C})=7.458\text{MeV}$ , which would mainly *sequentially* decay with  $3\alpha$  of equal energies: a counterintuitive result of tunneling. Such a state, if it would exist, is at least 3 orders of magnitude less probable than the Hoyle’s, thus below the sensitivity of recent and past experiments.

[1] H. Zheng *et al.*, Phys. Lett. B **779**, 460 (2018).